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1 **Mechanical Property Measurements Enabled by Short Term Fourier** 2 **Transform of Atomic Force Microscopy Thermal Deflection Analysis**

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9 **Abstract**

10 Contact resonance atomic force microscopy (CR-AFM) has been used in many studies to charac-
11 terize variations in the elastic and viscoelastic constants of materials along a heterogeneous sur-
12 face. In almost all experimental work, the quantitative modulus of the surface is calculated in ref-
13 erence to a known reference material, rather than calculated directly from the dynamics models of
14 the cantilever. We measure the cantilever displacement with very high sampling frequencies over
15 the course of the experiment and capture its oscillations that result from thermal energy. Using
16 short term Fourier transformations (STFT), it is possible to fit the thermal resonance peak of the
17 normal displacement to track the frequency and Q-factor of the cantilever during an experiment,
18 using a similar process to that used to calibrate the normal bending stiffness of cantilevers. With
19 this quantitative data, we have used the dynamic mechanics models relating the contact stiffness of
20 the tip/cantilever pressing into a surface with the oscillation frequency of the cantilever and show
21 that they do not accurately model the experiment. Several material combinations of tip and sample
22 are examined, as well as tip size and cantilever stiffness demonstrate that existing models cannot
23 capture the physics of this problem.

24 **Keywords**

25 atomic force microscopy; contact resonance; highly oriented pyrolytic graphite (HOPG); mechani-
26 cal property measurements; surface science

27 **Introduction**

28 Atomic force microscopy (AFM) has become an indispensable tool for imaging surface topogra-
29 phy on a variety of surfaces [1]. Since the invention of the AFM [2], several other modes of AFM
30 have been developed, including friction force microscopy [3], tapping mode AFM [4], contact res-
31 onance AFM (CR-AFM) [5], etc., each providing unique advantages or insights into a surface and
32 the materials that comprise it. Alongside the developments of the experimental technique has been
33 a number of modeling techniques that can be used to bring physical values or interpretation to the
34 data that is collected by the AFM, allowing operators of the technique to compare their measure-
35 ments across fields [6].

36 CR-AFM is a technique that was established in 2008 allowing for the measurement of mechani-
37 cal properties (elastic modulus and viscoelastic modulus) of surfaces [5]. It is particularly useful
38 for the measurement of heterogeneous surfaces, characteristic of composite and biological mate-
39 rials, where understanding the interplay between microstructure and mechanical properties of the
40 constituent materials is critical for the performance of the overall structure. Analytical models for
41 interpreting the vibrational modes of cantilevers were developed prior to the invention of the tech-
42 nique [7,8]. This model or a variation of it is often presented in manuscripts to explain the inter-
43 pretation of experimental data, but is not used to bring physical meaning to the experimental data.
44 Instead, in almost every example in the literature, the frequency variation is normalized to what is
45 measured on a surface having known mechanical properties [5,9,10].

46 Alongside the development of CR-AFM and the analytical models that have been used to describe
47 the technique, spectral analysis of the thermal motion in the deflection of AFM cantilevers has
48 shown promise as a lower-cost or less equipment-intensive mechanism to access the dynamic and
49 time-evolving properties of the cantilever [11-13]. In these techniques, the cantilever deflection

50 signal is acquired at rates several times greater than the first normal resonant frequency (typically
51 greater than 1 MHz) for several seconds, as the cantilever is approached, pressed against, and re-
52 moved from a surface. Primarily, wavelet transformations of the AFM cantilever's deflection sig-
53 nal has been reported that show variations in the cantilever's contact resonant frequency over the
54 course of the experiment that could be linked to mechanical property variations arising from con-
55 fined fluids that order, etc [11-13]. However, quantitative measurement or conversion of the mea-
56 sured frequency of the AFM cantilever's bending mode, have not realized at this point.

57 In this manuscript, we bring together the analytical models that describe cantilever oscillations in
58 AFM experiments where a tip is oscillated and pressed into contact with a solid surface [7,8] with
59 the spectral analysis of the thermal motion of the cantilever. By examination of the thermal os-
60 cillations of the AFM cantilever, we can make very small perturbations that are sub Ångström in
61 displacement, or much smaller than atomic bonds in our materials. We also avoid disturbance of
62 the medium surrounding the sample, as is done with photo-thermal excitation, without expensive
63 modification to our existing AFM system. Finally, by avoiding using a phase locked loop to track
64 the frequency of the cantilever oscillation, we are able to track the oscillation of the cantilever as
65 it changes from a free out-of-contact to in-contact oscillator. Additionally, spectral analysis allows
66 for the measurement and tracking of all resonant modes simultaneously, which would otherwise
67 require a phase locked loop for each mode that is to be tracked.

68 To realize these goals, we have conducted AFM experiments on well-characterized surfaces, such
69 as highly ordered pyrolytic graphite (HOPG), and silicon cantilevers. Short term Fourier trans-
70 forms, rather than wavelet transforms, are used as the mathematical relationship linking the oscilla-
71 tion parameters and AFM cantilever and the spectral resolution required to accurately capture these
72 parameters are well-documented. Then the analytic models used to interpret CR-AFM experiments
73 are outlined. We then present experimental data on several surfaces are analyzed and their align-
74 ment with the analytic models are presented.

75 **Methods**

76 **Experiment Design**

77 An Agilent Keysight 5500 AFM was used in all experiments with measurements conducted un-
78 der ambient laboratory conditions of 20-40% humidity. Four samples were analyzed in the exper-
79 iments: a silicon wafer, freshly-cleaved highly ordered pyrolytic graphite (HOPG), poly(ethylene
80 oxide) (PEO), and polydimethylsiloxane (PDMS). The mechanical properties of these samples are
81 provided in Table 1 below:

Table 1: Mechanical properties of the examined samples. Values for silicon and HOPG are from Refs [14] and [15]. The values for PEO and PDMS were measured using a Hysitron Premier Nanoindenter.

Material	Young's Modulus (GPa)	Poisson's Ratio
Silicon	160	0.3
HOPG	20	0.25
PEO	0.22 ± 0.03	0.5
PDMS	0.0025 ± 0.0002	0.45

82 Silicon wafers were ultrasonicated in acetone and subsequently again in ethanol for 10 minutes
83 each. HOPG samples were cleaved using the scotch tape method within 30 minutes of beginning
84 an experiment. Finally, the PEO and PDMS samples were not surface treated following their poly-
85 merization/deposition. The topography of the surface was measured before acquiring a force versus
86 distance measurement to ensure that these measurements were acquired on clean and flat regions
87 of the substrate. Force versus distance measurements were acquired by moving the sample up and
88 down at a rate of approximately 100 nm/s and recording the cantilever deflection over the course of
89 the measurement. In addition to the AFM's own control software measuring the deflection of the
90 cantilever over the experiment, the cantilever deflection was measured by a National Instruments
91 BNC box (NI-USB-6341) via an unfiltered connection direct from the photodetector at 2.0 MHz
92 and for 1s duration of the experiment, unless otherwise noted. The data from this instrument will
93 be referred to in the paper as the "high-sample rate" data.

94 Three types of uncoated cantilevers were used all experiments: soft cantilevers with an integrated

95 tip (Nanosensors PPP-CONT), soft tipless cantilevers (Nanosensors TL-CONT), and harder can-
 96 tilevers with an integrated tip (Nanosensors PPP-NCL). The soft cantilevers have a nominal stiff-
 97 ness in the normal bending direction of 0.2 N/m and the hard cantilevers have a nominal stiffness
 98 of 40 N/m. For each cantilever used, in the normal bending direction was determined through
 99 the Sader method [16], with the plan-view dimensions and the setback of the tip from the end
 100 of the cantilever measured in an optical microscope. To convert the voltage signal measured by
 101 the photodetector, the slope of the force versus distance curve generated from the manufacturer's
 102 software was determined, having units of V/m. Four different tip materials were used in experi-
 103 ments: conventional silicon cantilevers (Nanosensors PPP-CONT), conductive diamond coated
 104 probes (Nanosensors CDT-CONTR), platinum silicide coated probes (Nanosensors PtSi-CONT),
 105 and borosilicate glass colloids (Sigma-Aldrich 440345-100G) attached to the tipless cantilevers
 106 (Nanosensors TL-CONT). The borosilicate glass colloids had a diameter of 8-11 μm and an elastic
 107 modulus of 60 GPa.

108 **Data Analysis**

109 Following completion of experiments, post processing of the high sample rate data was performed.
 110 This data was windowed into segments of data having length of 2^N in number of data points, with
 111 N ranging from 10-20. These windowed segments were convolved with the Hanning window to
 112 reduce spectral leakage. For each window, a Fourier transform was calculated and stored. Subse-
 113 quently, for each window generated the resonant peak of the first normal mode was fit using eq. (1),

$$114 \quad A(f) = \frac{k_B T f_n^3}{\pi Q_n D_n (f^2 - f_n^2)^2 + (\frac{f f_n}{Q_n})^2} \cdot 10^{18} + y_0 \quad (1)$$

115 where f is the frequency, T is the temperature, $k_B = 1.3806 \times 10^{-23} \text{ m}^2\text{kg}\cdot\text{s}^{-2}\text{K}^{-1}$ is Boltzmann's
 116 constant, (Q_n) is the quality factor of the cantilever for the n -th mode, D_n is the stiffness of the n -th
 117 oscillation mode, and y_0 is an offset value [17]. Fits of these resonant peaks using the non-linear
 118 least squares method yielded parameters f_n , Q_n , and D_n . To ensure accurate fits to the resonance

119 peak, the window size N , impacting the frequency resolution (f_Δ) of the calculated Fourier trans-
120 form, was carefully chosen to ensure that β in eq. (2) was much larger than 1 [18].

$$121 \quad \beta = \frac{\pi}{2Q_n} \frac{f_n}{f_\Delta} \quad (2)$$

122 Fitting of the first resonant peak of the cantilever in contact with the surface during the force versus
123 distance measurement thus provides a time evolution of the f_1 , Q_1 , and D_1 values as a function of
124 time during the experiments. These values can be related to the displacement of the sample, force,
125 etc. that is time averaged over the window size, thus can be correlated.

126 **Analytical Models of Cantilever Dynamics**

127 Several analytical models of cantilever dynamics have been developed, with the basis of most mod-
128 els originating from the work by Rabe *et al.* in Ref. [7], and are schematically shown in Figure 1
129 (a) (i) and (ii). More advanced models have been subsequently developed that include the tilt angle
130 of the cantilever relative to the surface [19], to better reflect the typical 12.5° or 22.5° angle of the
131 cantilever relative to the surface, are shown in Figure 1 (a) (iii). To relate the oscillation frequency
132 of the cantilever to the contact stiffness, equations of motion for the schematic have been developed
133 in Refs [7,19]. and are provided in the SI for reference. These equations are used to develop the
134 dispersion curve, shown in Figure 1 (b). The dispersion curve shows how the measured frequency
135 changes as the contact becomes stiffer, which occurs as a result in the previously described experi-
136 ments by the tip pressing with a larger normal force against the surface. In CR-AFM experiments,
137 typically experiments are conducted at a constant normal force (increasing the tip-sample contact
138 size), and thus changes in the contact stiffness results from variations in the elastic modulus, E ,
139 along the surface. The relation between elastic modulus, contact size, and contact stiffness is found
140 in eq. (3) [20],

141

$$k^* = 2aE^* \quad (3)$$

142

$$\frac{1}{E^*} = \frac{1 - \nu_{sample}^2}{E_{sample}} + \frac{1 - \nu_{tip}^2}{E_{tip}^*} \quad (4)$$

143

where a is the size of the contact between the tip and sample, E^* is the reduced elastic modulus

144

defined in eq. (4), ν is the Poisson ratio of the tip or sample, and E is the elastic modulus of the tip

145

or sample.

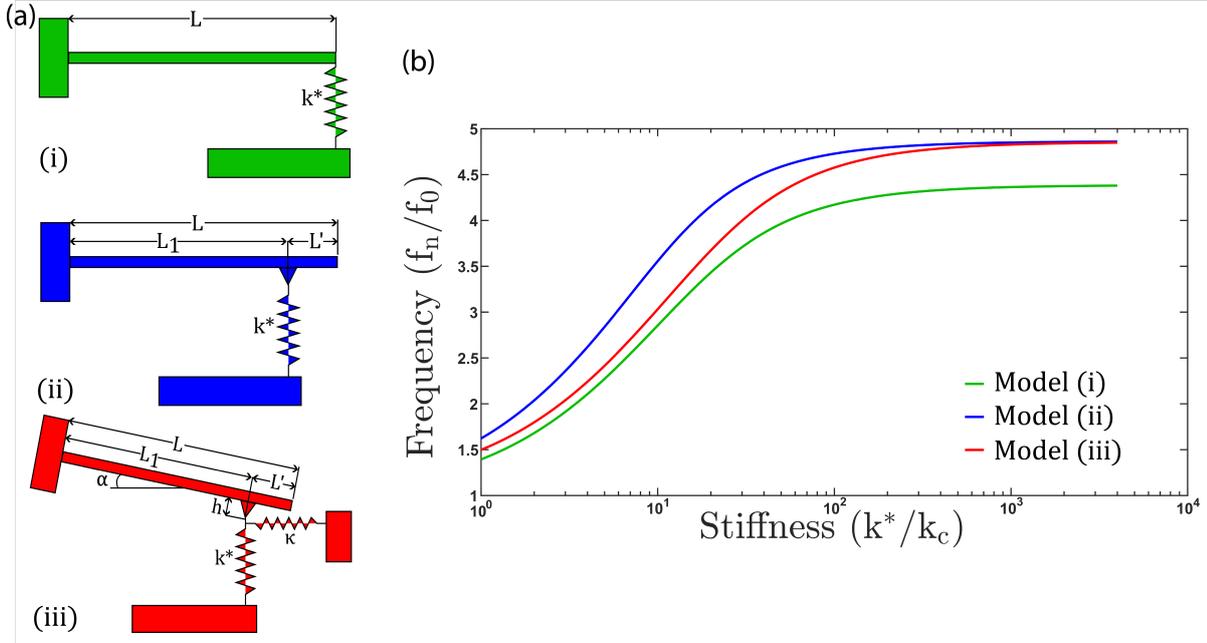


Figure 1: (a) Schematic diagrams of the cantilever models used in determining the dispersion curves to convert measured cantilever oscillation frequency to contact stiffness of the tip-sample contact. Three models are typically used: (i) shows the tip at the end of the cantilever, (ii) shows the tip set back from the end of the cantilever, and (iii) shows a cantilever tilted with respect to the surface and the tip set back from the end of the cantilever. L is the overall cantilever length, L' is the distance that the tip is set back from the end of the cantilever, k^* is the contact stiffness, α is the tilt angle of the cantilever with respect to the surface, h is the distance between the tip apex and the cantilever base, and $\kappa = 8G^*a$ (Ref. [19]) is the lateral stiffness of the tip-sample contact. (b) Dispersion curves providing a lookup table for the conversion of measured resonant frequency to tip-sample contact stiffness. Model (i) is shown in black, (ii) in blue, and (iii) in red.

146 **Results and Discussion**

147 Figure 2 (a) shows an example force versus distance measurement acquired with the high sample-
148 rate acquisition system for a soft silicon cantilever and a HOPG substrate. Both the normal force
149 and cantilever displacement values are shown, as most AFM studies report normal force values, but
150 the power spectrum calculation requires the cantilever displacement values. Figure 2 (b) shows the
151 calculated Fourier transform/power spectrum of the cantilever displacement in the out-of-contact
152 portion of Figure 2 (a), or the data acquired from approximately 0s to 2s of the experiment. The
153 power spectrum clearly shows the first four oscillation modes of the cantilever, with the first oscil-
154 lation mode having the largest amplitude. Figure 2 (c) shows the quality of the fit obtained using
155 eq. (1) to the first oscillation mode, yielding values of $f_1 = 12.627 \pm 0.003$ kHz, $Q_1 = 19.84 \pm$
156 0.20 , and $D_1 = 25.67 \pm 0.02$ mN/m. We note that the fit value obtained from the eq. (1) is not the
157 the same value as obtained using the Sader method (74.3 mN/m for this cantilever in Figure 2) [16].
158 Similar observations were made for the other cantilevers used in the experiments conducted within
159 this paper, with the difference between the value of D_1 and the normal spring constant calculated
160 using the Sader method ranging between a factor of 2 and 10. This difference is likely a result of
161 the plan view dimensions of the cantilevers having dimensions beyond the 10% variation of the
162 manufacturer's specifications, observed in other experiments we have conducted outside this study.
163 While viscous damping from the ambient environment is not accounted for in eq. (1) and may also
164 be responsible for a small percentage of the difference between the two calculations of the spring
165 constants, our results highlight that the measurements of the cantilever's plan view dimensions and
166 using these dimensions in the determination of the Sader spring constant or other calculation of the
167 normal spring constant is important. Finally, it has been demonstrated that the Sader method can
168 consistently show a difference compared with the thermal noise method used above, particularly
169 for soft cantilevers as used in this study [21]. We take the Sader spring constant, which has been
170 widely used in other studies and is less sensitive to variations in the calculated cantilever sensitiv-
171 ity [21], as the spring constant of all cantilevers in the calculations in subsequent sections of this
172 manuscript.

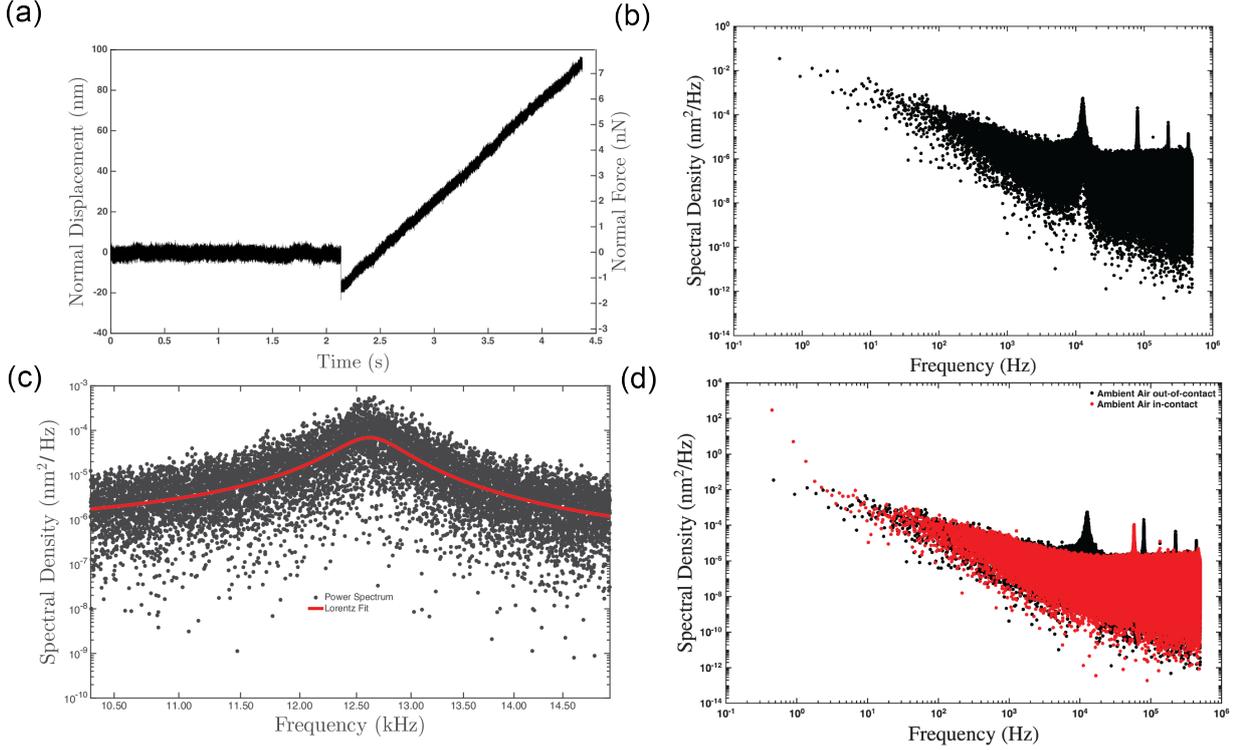


Figure 2: (a) Result of force versus displacement using the high sample rate acquisition system. (b) Fourier transform of the out-of-contact portion of (a). (c) Fit (red line) of the first resonant mode peak (black squares) with eq. (1). (d) Fourier transform of the out-of-contact portion of (a) shown in black and the in-contact portion shown in red, highlighting the change in the resonant peak locations and shapes between these two stages of the measurement. Data was acquired at 1 MHz for approximately 4.5s.

173 Figure 2 (d) shows two power spectra, the black spectrum calculated from the time ranging from
 174 0s to 2s, and the second in red from the time ranging between 2.5s and 4.5s. These two spectra
 175 highlight the change in the location and shape of the normal resonant peaks for the cantilever from
 176 when the cantilever was out-of-contact and when it was in contact. We are able to estimate the val-
 177 ues of the various modes, as Rabe *et al.* showed that the value of $\frac{f_n}{(k_n L)^2}$ is a constant for the can-
 178 tilever, which also allows us to distinguish between higher order oscillatory modes of the cantilever
 179 and pinning of the free end of the cantilever [7]. With the the first resonant peak out of contact hav-
 180 ing a center frequency of 12.62 kHz and using Model (i) to estimate the location of subsequent
 181 resonant peaks, the expected second resonant mode of a free cantilever would be approximately
 182 79.1 kHz, versus an expected frequency of 55.3 kHz in the first resonant mode if the end of the
 183 cantilever was completely pinned. The measured value of the cantilever resonant frequency when

184 the tip was pressed into the surface was 58.15 kHz, which is much closer to the expected value of
185 pinned cantilever than the second resonant mode. Beyond identifying and fitting the first pinned
186 mode of oscillation, it is also possible to observe several of the higher modes within the in-contact
187 power spectrum compared with the out-of-contact spectrum. Finally, we note that the full width at
188 half maximum increases slightly for the first oscillation mode when the cantilever makes contact
189 with the surface, but shows significant scatter during the force curve measurement, making a state-
190 ment regarding the variation of the Q -factor difficult with the present analysis technique.

191 Figure 3 (a) shows the variation of the frequency of the first normal mode as a function of normal
192 force during the in-contact portion of the force curve. A sub-linear variation is observed with in-
193 creasing applied normal force. Figure 3 (b) shows the variation of the quality factor with normal
194 force, simultaneously determined with the frequency of the frequency of the first normal oscillatory
195 mode. Here, the variation in the Q -factor is less clear than for the resonant frequency: an initial
196 increase is observed, that plateaus around 0 nN applied force. However, significant scatter in the
197 Q -factor is observed, in particular compared with the variation in the frequency of the first normal
198 oscillatory mode. Significantly more scatter is observed for the last fit parameter, D_1 , which in the
199 case of a free oscillation represents the spring constant of the single-harmonic-oscillator mode.

200 There is significant scatter in the value of D_1 during in-contact measurements, and thus has been
201 included in the SI (Fig. S1) for completeness.

202 Figure 4 shows the dispersion curves generated for the three cantilever models, with the data ob-
203 tained from all material combinations evaluated in this study in each of the models. For example,
204 Figure 4 shows that for soft materials, such as the Si-PDMS combination (silicon cantilever, PDMS
205 substrate), all three models can be used to translate the oscillation frequency variation into a con-
206 tact stiffness. However, for harder materials, such as Si-HOPG or Diamond-Si, Model 1 (Figure 1
207 (i)) has a frequency response in the dispersion curve that saturates at a reduced frequency (f_1/f_0)
208 that is lower than the measured reduced frequency. Model 3 (Figure 1 (iii)) in this case does not
209 saturate as early, but the plateau in the dispersion curve translates into a wide variation in contact
210 stiffness values assigned for very small changes in frequency. Thus, Model 2 does not have suf-

211 ficient accuracy for contact stiffness determination for these material systems. Model 2 (Figure 1
 212 (ii)) slightly improves upon this issue, with the dispersion curve shifted more significantly to lower
 213 values of contact stiffness and a higher frequency plateau than Model 1, such that improved ac-
 214 curacy in translating the measured cantilever frequency to a stiffness is possible. The additional
 215 benefit of Model 2 over Model 3 is that the model is much simpler and a friction coefficient, κ , be-
 216 tween the tip/colloid and the substrate does not need to be assumed or calculated to generate the
 217 dispersion curve. However, as shown in Figure 1, the value of κ does not significantly change the
 218 positioning of the dispersion curve.

219 It has been suggested that careful selection of the cantilever stiffness is required when performing
 220 CR-AFM measurements [22]. Within the context of Figure 1, increasing the value of k_c while all
 221 other material parameters remaining constant should shift the measured reduced frequency (f_n/f_0)
 222 left or to lower values, to a region of the dispersion curve where a more linear variation between
 223 frequency and stiffness is expected. In other words, with a very soft cantilever and a very hard sam-
 224 ple, the saturated variation of the reduced frequency changes very little with contact stiffness, k^* .
 225 We attempted to use cantilevers with a higher k_c value, ranging from 20-40 N/m to perform the
 226 same analysis as done previously. As shown in Fig. S2, the issue becomes that with the stiffer can-
 227 tilever, the magnitude of the resonance peak for the first normal mode, particularly when the tip
 228 contacts the surface, is much smaller than for the softer cantilevers. At this time, the base noise of
 229 our AFM system and electronic sampling of the deflection signal is too large to automate the fitting
 230 of the resonance peak with reasonable successful fits.

231 With the frequency data translated to contact stiffness, the DMT, JKR, and Carpick-Ogletree-
 232 Salmeron (COS) contact mechanics theories can be used to then relate the tip size, elastic modulus,
 233 and normal force. The relationship between contact stiffness, k^* , and normal force for the DMT,
 234 JKR, and COS models are then given by eq. (5), eq. (6), and eq. (7), respectively [20,23].

$$235 \quad k_{DMT}^* = 2E^* \left(\frac{R(3F + F_a)}{4E^*} \right)^{1/3} \quad (5)$$

$$k_{JKR}^* = 2E^* \left(\frac{3R(3F + 2F_a + \sqrt{4FF_a + 4F_a^2})}{2E^*} \right)^{1/3} \quad (6)$$

$$k_{COS}^* = 2E^* \left(\frac{\hat{a}_o}{\hat{F}_c^{1/3}} \right) \left(\frac{R(3F + F_a)}{4E^*} \right)^{1/3} \quad (7)$$

238 where R is the tip radius and F_a is the adhesive force. In eq. (7), we use the transition parame-
 239 ter, λ , bridge the two contact streams. We then denote $\hat{a}_o = a \cdot \left(\frac{E^*}{\pi\gamma R^2} \right)^{1/3}$ and $\hat{F}_c = \frac{F}{\pi\gamma R^2}$, and
 240 γ is the work of adhesion, which can be calculated from the pull-off force in experiments. We
 241 calculated the Tabor parameter and the λ -parameter for each material pair and given in Table 2.
 242 Rather than fitting data with Tabor parameter less than 0.1 with the DMT model and greater than
 243 5 with the JKR model [24], we use the COS model that has been shown to more accurately fit con-
 244 tacts having material properties between the DMT and JKR extremes. The fits to the experimen-
 245 tal data are provided in Figure 5. In each case, all materials for the tip and substrate were pure
 246 amorphous/polycrystalline, and thus had homogeneous elastic moduli across the surface. Fur-
 247 ther, these materials were chosen as they are well-characterized in the literature and often used
 248 in AFM experiments. Thus, rather than fitting the elastic modulus of the substrate, we took the
 249 elastic modulus values from literature for the tip and substrate and fit the radius of the probes us-
 250 ing contact mechanics models. In many cases the fits did not converge, so we have used the best
 251 fit values near convergence and plotted the expected model variations for k^* and normal force in
 252 Figure 5 in a red dashed line with the experimental data overlaid in the graph. In each case, as
 253 stated previously, either the fit did not converge, or yielded unphysical values for the tip radius.
 254 More specifically, Figure 5 (a) and (b) show converging fits to the experimental data, resulting in
 255 a fit of 0.02580 ± 0.00002 nm and 17.42 ± 0.13 nm, respectively. Figure 5 (c) and (d) show results
 256 where the fit did not converge, with the experimental results clearly not following the predicted
 257 trend for contact stiffness by the MG model. In these cases the radius estimated for the fit shown in

258 Figure 5 (c) and (d) was 0.0011 nm and 0.092 nm, respectively. This result is a result of the very
 259 high stiffness of the contacting materials that resulted in the reduced frequency having a value near
 260 the asymptote of the dispersion curve in Model (ii) and (iii).

Table 2: Tabor and transition parameters calculated for each material pairing.

Probe Material	Sample Material	Tabor μ_T	Transition λ
Silicon	HOPG	0.4567	0.5284
Diamond	Silicon	0.16	0.1851
Glass Colloid	HOPG	7.1923	8.3214
Steel Colloid	Silicon	1.8955	2.1931
Silicon	PEO	3.1962	3.6980
Silicon	PDMS	283.961	328.543

261 Figure 6 shows SEM images of two of the tips used in the study: a borosilicate glass colloid glued
 262 onto a tipless silicon cantilever and a PtSi coated silicon cantilever. In each of these cases, the tip
 263 radius was estimated to be much larger than what was fit in Figure 5. While it is possible that, in
 264 particular with the colloid probe, local surface roughness will have a much smaller contact radius
 265 than the overall probe shape, it is still significantly larger than predicted by the models in Figure 5.
 266 In summary, we have used longstanding analytical models to convert the measured variation in can-
 267 tilever resonant frequency with applied normal force into contact stiffness. While the measurement
 268 process is very similar to what is typically done in CR-AFM studies, it becomes more clear as to
 269 why these studies normalize their results to a section or area of the surface with known mechanical
 270 properties: the analytical models that have been developed do not accurately describe the variation
 271 of cantilever frequency when the tip is pressed against the surface. At this time, no better mod-
 272 els were developed to describe the link between cantilever frequency and contact stiffness, and we
 273 believe that normalization of the surface properties is the only method that it is possible for experi-
 274 mentalists to provide some understanding of a quantitative value of the surface elastic modulus and
 275 other mechanical properties.

276 **Conclusions**

277 High data rate acquisition of the cantilever deflection signal from the photodiode of an AFM al-
278 lows for the capture of the thermal motion of the AFM cantilever during a force versus distance
279 measurement. STFT analysis was used to produce power spectra at regular time intervals during
280 the experiments, with the frequency resolution varied to balanced against the desire to have a faster
281 time response of the cantilever's oscillation parameters and the necessary frequency resolution to
282 accurately fit the resonant peak of the first normal oscillation mode of the AFM cantilever. The
283 resonance mode was fit to a Lorentz peak to extract its center frequency and quality factor at each
284 time point, providing similar information as to what is generated in a CR-AFM experiment. The
285 cantilever resonant frequency was then converted into contact stiffness using analytical models
286 of cantilever vibrations, which could then be compared with contact mechanics models relating
287 the applied normal force to contact stiffness. It was shown that those commercially available can-
288 tilevers, which provide enough signal for analysis in a standard AFM, push CR-AFM into a regime
289 where small variations in frequency result in large variations of derived contact stiffness. This re-
290 lationship between frequency and contact stiffness makes correlating experimental contact reso-
291 nance data with contact stiffness, or other mechanical property assessment, very difficult. Thus,
292 our findings show that, while high fidelity data of the changing oscillatory behavior of AFM can-
293 tilevers can be obtained with high sampling rates and subsequent STFT analysis, quantitative analysis
294 is not possible without measuring calibration curve or normalizing data on a known material pair.
295 These observations confirm why most CR-AFM studies report normalized data, despite providing
296 information on the analytical models to convert frequency to contact stiffness in most cases, or only
297 show qualitative frequency data.

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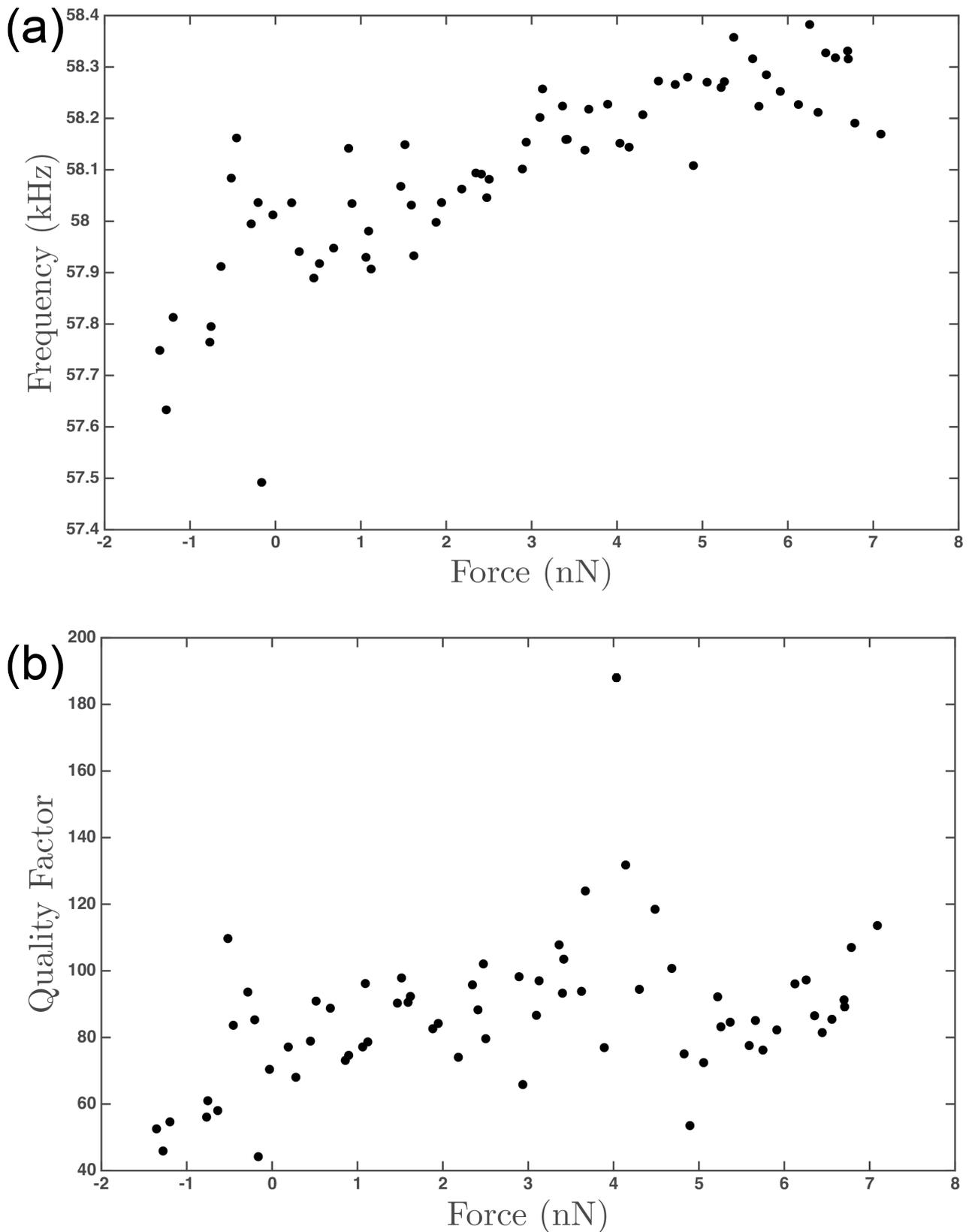


Figure 3: (a) Resonant frequency versus normal force determined from fits of the first normal resonant mode peak in the power spectra of the contact portion of Figure 2. (b) Quality factor (Q) versus normal force similarly determined from the power spectra of the contact portion of Figure 2. $N=17$ in (a) and (b).

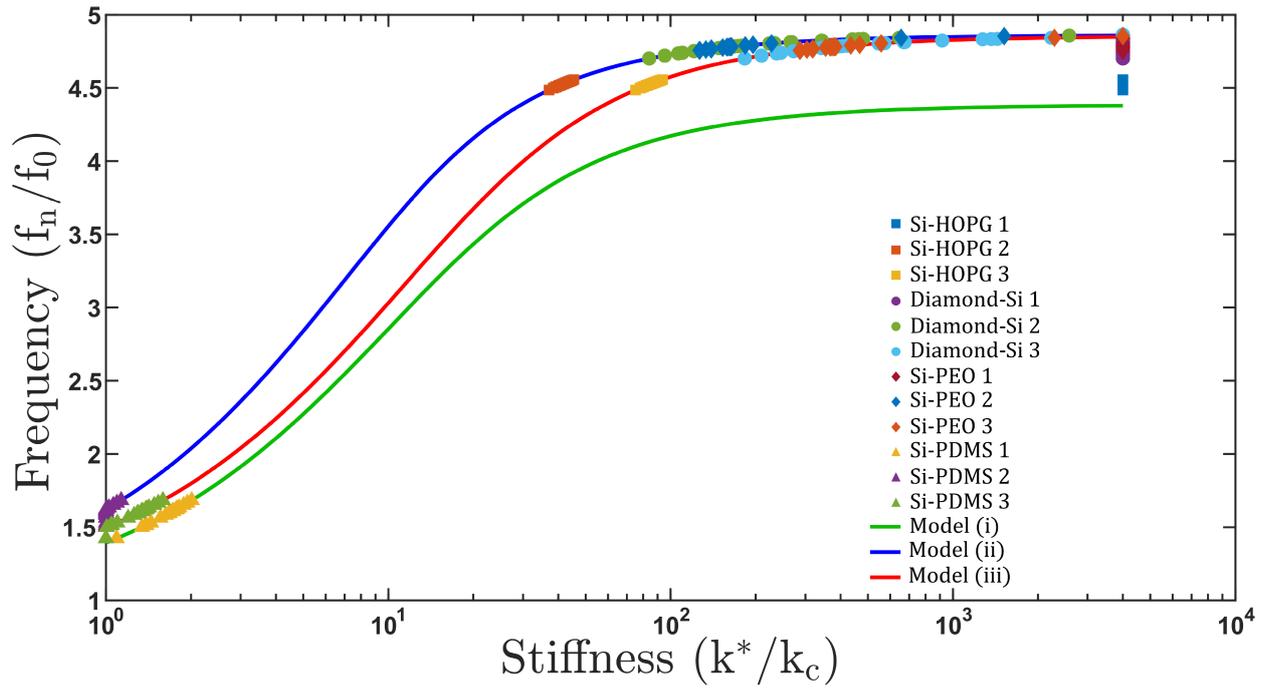


Figure 4: Experimental data for all sample combinations tested (silicon tips vs. HOPG substrate, diamond coated tips on silicon substrate, silicon tip on PEO, silicon tip on PDMS) plotted for the three cantilever models.

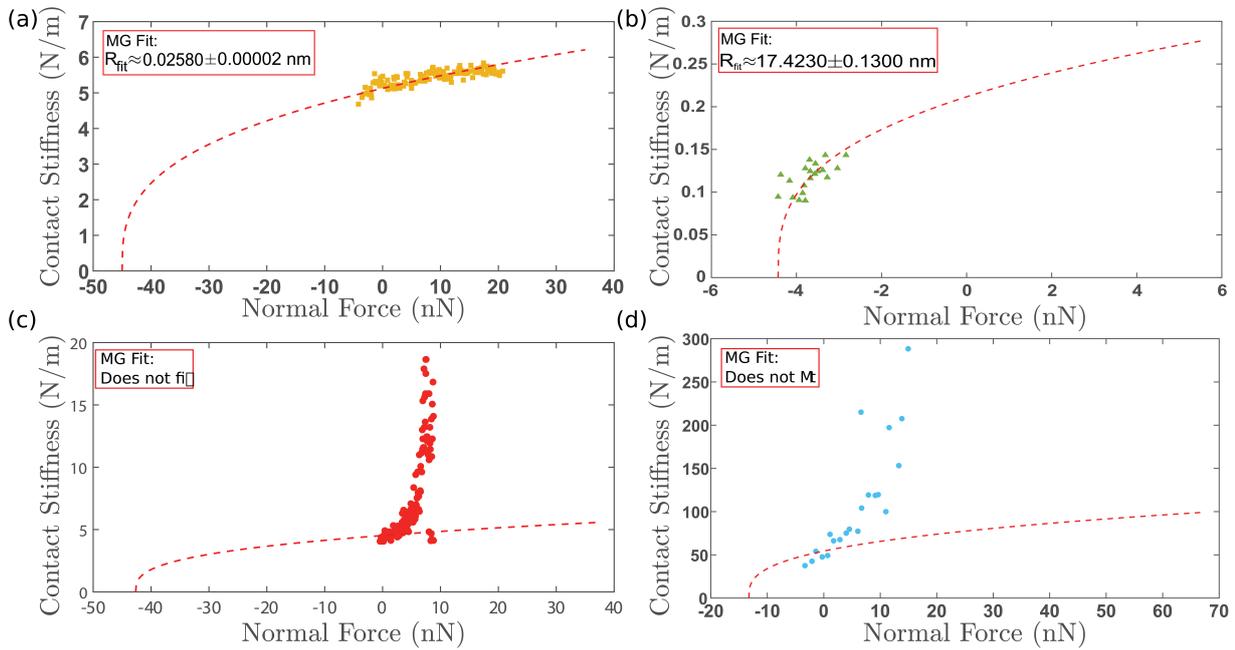


Figure 5: Contact stiffness versus normal force for (a) a silicon probe on HOPG sample (yellow squares) (b) a silicon probe on PDMS sample (green triangles), (c) a borosilicate glass colloid probe on a HOPG sample (red circles), and (d) a diamond coated silicon on silicon sample (blue circles). A red dashed line in each figure shows a fit to the experimental data using eq. (7).

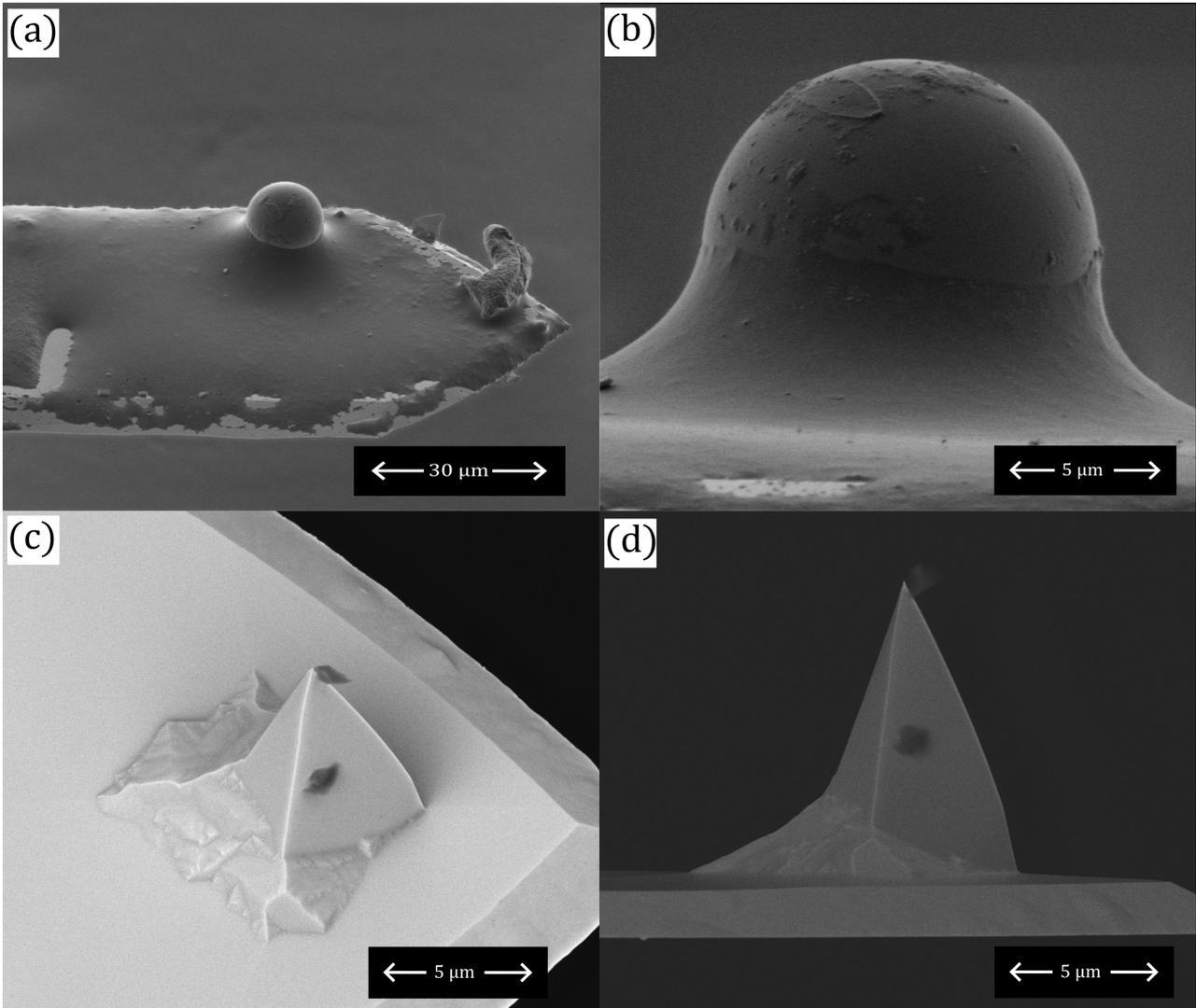


Figure 6: (a) and (b) Scanning electron images of the borosilicate glass colloid glued on the tip-less silicon cantilever. (c) and (d) Scanning electron microscope image of PtSi coated AFM cantilever with integrated tip.